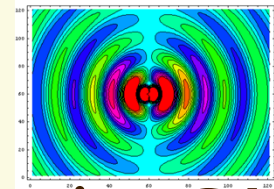




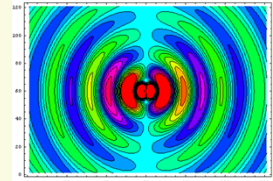
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TÉCNICO



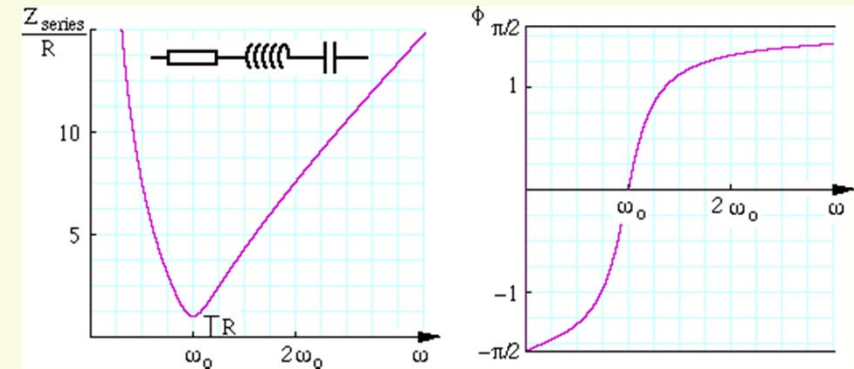
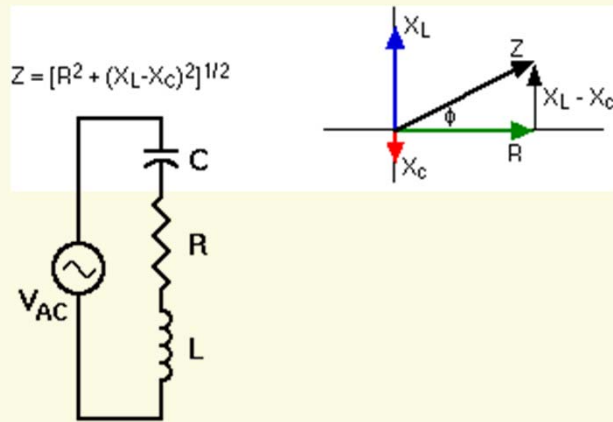
Aula 14: Circuitos CA

- 14.1. Circuito RLC série**
- 14.2. Circuito RLC paralelo**
- 14.3. Ressonância no circuito RLC**
- 14.4. O factor de qualidade do circuito RLC**
- 14.5. Impedâncias complexas**

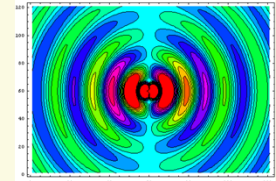
Circuito RLC série: animação



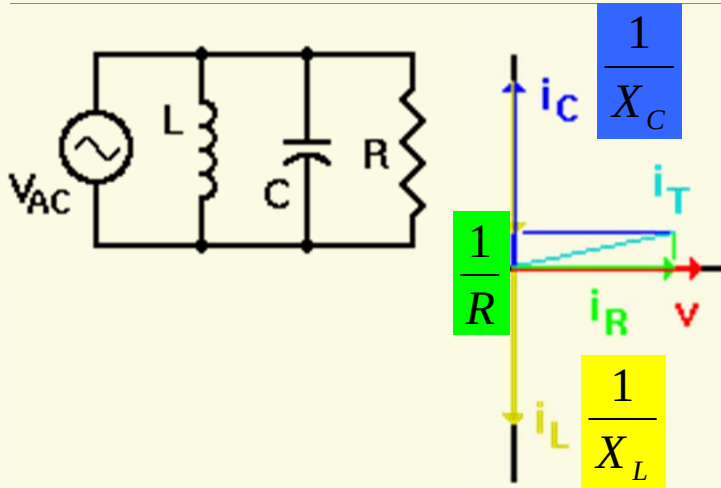
14.1. Circuito RLC série



$$Z_{\text{series}} = \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2} \quad \phi = \tan^{-1} \frac{\omega L - 1/\omega C}{R}$$



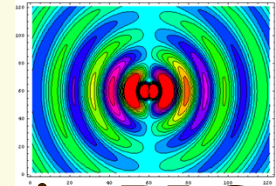
14.2. Circuito RLC paralelo



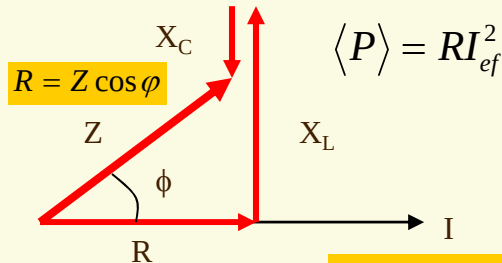
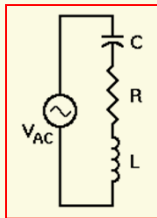
$$\tan \varphi = \frac{\frac{1}{X_C} - \frac{1}{X_L}}{\frac{1}{R}} \quad \frac{1}{Z} = \sqrt{\frac{1}{R^2} + \left(\frac{1}{X_C} - \frac{1}{X_L} \right)^2}$$

$$I_{\max} = \frac{\mathcal{E}_{\max}}{Z} = \mathcal{E}_{\max} \sqrt{\frac{1}{R^2} + \left(\frac{1}{X_C} - \frac{1}{X_L} \right)^2}$$

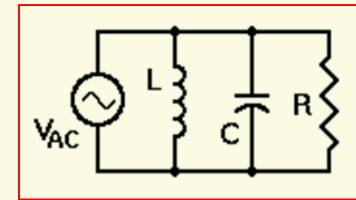
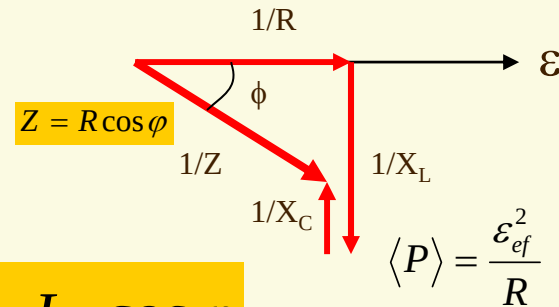
Simulação: condição de ressonância

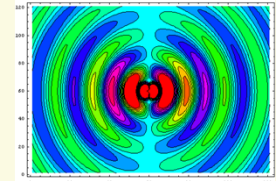


14.3. Ressonância no circuito RLC

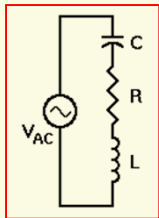


$$\langle P \rangle = \mathcal{E}_{ef} I_{ef} \cos \varphi$$





14.4. O factor de qualidade do circuito RLC



$$\langle P(\omega) \rangle = \frac{R\omega^2 \mathcal{E}_{ef}^2}{L^2(\omega^2 - \omega_0^2)^2 + R^2\omega^2}$$

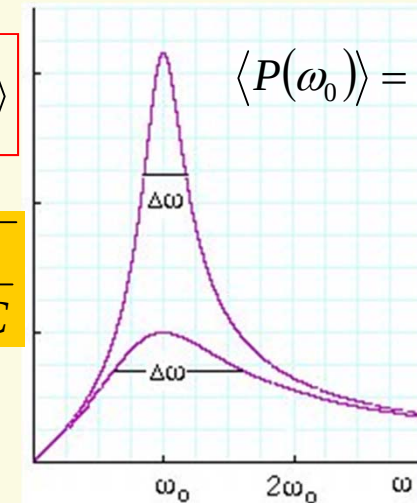
$$\langle P(\omega) \rangle = \frac{1}{2} \langle P(\omega_0) \rangle$$

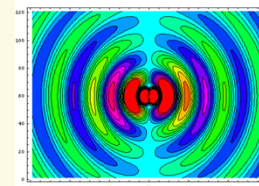
$$\langle P(\omega_0) \rangle = \frac{\mathcal{E}_{ef}^2}{R}$$

Factor de qualidade:

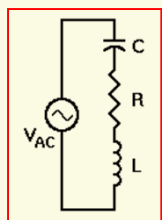
$$Q = \frac{\omega_0}{\Delta\omega} \Leftrightarrow Q = \frac{L\omega_0}{R} = \frac{1}{R} \sqrt{\frac{L}{C}}$$

Largura da banda: $\Delta\omega = \frac{R}{L}$



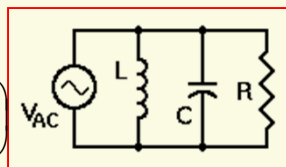


14.5. Impedâncias complexas

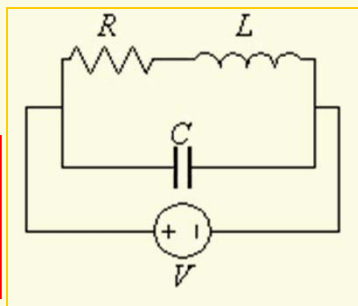


$$Z = R + i \left(L\omega - \frac{1}{C\omega} \right)$$

$$\frac{1}{Z} = \frac{1}{R} + i \left(C\omega - \frac{1}{L\omega} \right)$$

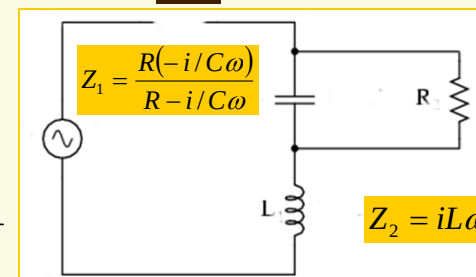


$$Z_1 = R + iL\omega \quad Z_2 = -i/C\omega$$



$$Z = \frac{Z_1 Z_2}{Z_1 + Z_2}$$

$$C = \frac{L}{R^2 + L^2 \omega^2}$$



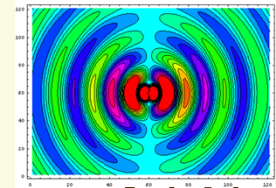
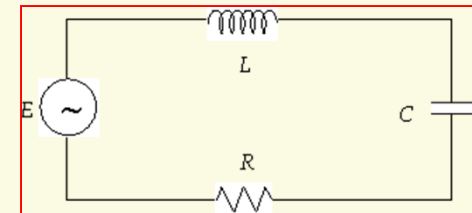
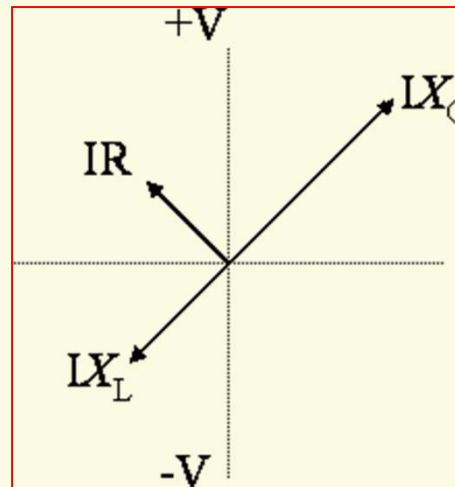
$$Z = Z_1 + Z_2 \quad L = \frac{R^2 C}{R^2 C^2 \omega^2 + 1}$$

Ressonância: $\varphi = 0$

Considere o diagrama vectorial das quedas de potencial nos elementos R, L e C do circuito RLC série representado na Figura.

Qual o valor da frequência ω da corrente alternada em relação à frequência de ressonância ω_0 do circuito?

- A** $\omega > \omega_0$
- B** $\omega < \omega_0$
- C** $\omega = \omega_0$

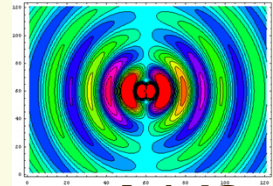


Teste A141

O esquema do circuito colector (pickup) de uma guitarra eléctrica está representado na Figura.

Qual o valor da impedância Z do circuito pickup para as frequências $\omega = 0$ e $\omega = \infty$ das cordas da guitarra?

- A** $Z(\omega=0) = 0$ ohms and $Z(\omega=\infty) = 0$ ohms
- B** $Z(\omega=0) = 0$ ohms and $Z(\omega=\infty) = R$ ohms
- C** $Z(\omega=0) = R$ ohms and $Z(\omega=\infty) = 0$ ohms



Teste A142

